1. Will the fish reach the next bowl?

- Jumping point from the lower bowl is the origin $(0,0)$
- Flight path is parabolic
- Next bowl is 2 units up, 3 units to the right, and 2.5 units wide

a) At desmos.com/calculator represent the upper bowl:

$$
y=2\{3<x<6.5\}
$$

b) Which flight paths cross the above line segment? Restrict to $\{y>0\}$.

$$
\begin{array}{ll}
f(x)=-(x-1)^{2}+1 & f(x)=-\frac{1}{2}(x-1)^{2}+\frac{1}{2} \\
f(x)=-(x-2)^{2}+4 & f(x)=-\frac{1}{2}(x-2)^{2}+2 \\
f(x)=-(x-3)^{2}+9 & f(x)=-\frac{1}{2}(x-3)^{2}+\frac{9}{2} \\
f(x)=-(x-4)^{2}+16 & f(x)=-\frac{1}{2}(x-4)^{2}+8
\end{array}
$$

2. Plot the parabolas on a computer to determine what the parameters $a, h$, and $k$ represent graphically.

$$
y=a(x-h)^{2}+k
$$

$f(x)=1(x-0)^{2}+0$
$f(x)=2(x-0)^{2}+0$
$f(x)=1(x-5)^{2}+0$
$f(x)=1(x-0)^{2}+5$
$f(x)=3(x-0)^{2}+0$
$f(x)=1(x-10)^{2}+0$
$f(x)=1(x-0)^{2}+10$
$f(x)=\frac{1}{2}(x-0)^{2}+0$
$f(x)=1(x+5)^{2}+0$
$f(x)=1(x-0)^{2}-5$
$f(x)=\frac{1}{3}(x-0)^{2}+0$
$f(x)=1(x+10)^{2}+0$
$f(x)=1(x-0)^{2}-10$
3. Plot these 3 satellite dish designs with a computer. Annotate the focus (focal point) at (h, $k+\frac{1}{4 a}$ ) on the computer. Freehand below.

$$
\begin{aligned}
& f(x)=\frac{1}{3}(x-0)^{2}+2\{y<3\} \\
& f(x)=\frac{1}{5}(x-5)^{2}+1\{y<2\} \\
& f(x)=\frac{1}{20}(x+10)^{2}+0\{y<1\}
\end{aligned}
$$

